

# *Fundamentals of Solid State Physics*

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# Preliminary Knowledge

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# Preliminary Knowledge

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## ■ Maths

- Calculus
- Linear algebra
- Probability and statistics

## ■ Physics

- Classical mechanics
- Electrodynamics
- Statistical mechanics
- Quantum mechanics

## ■ Chemistry

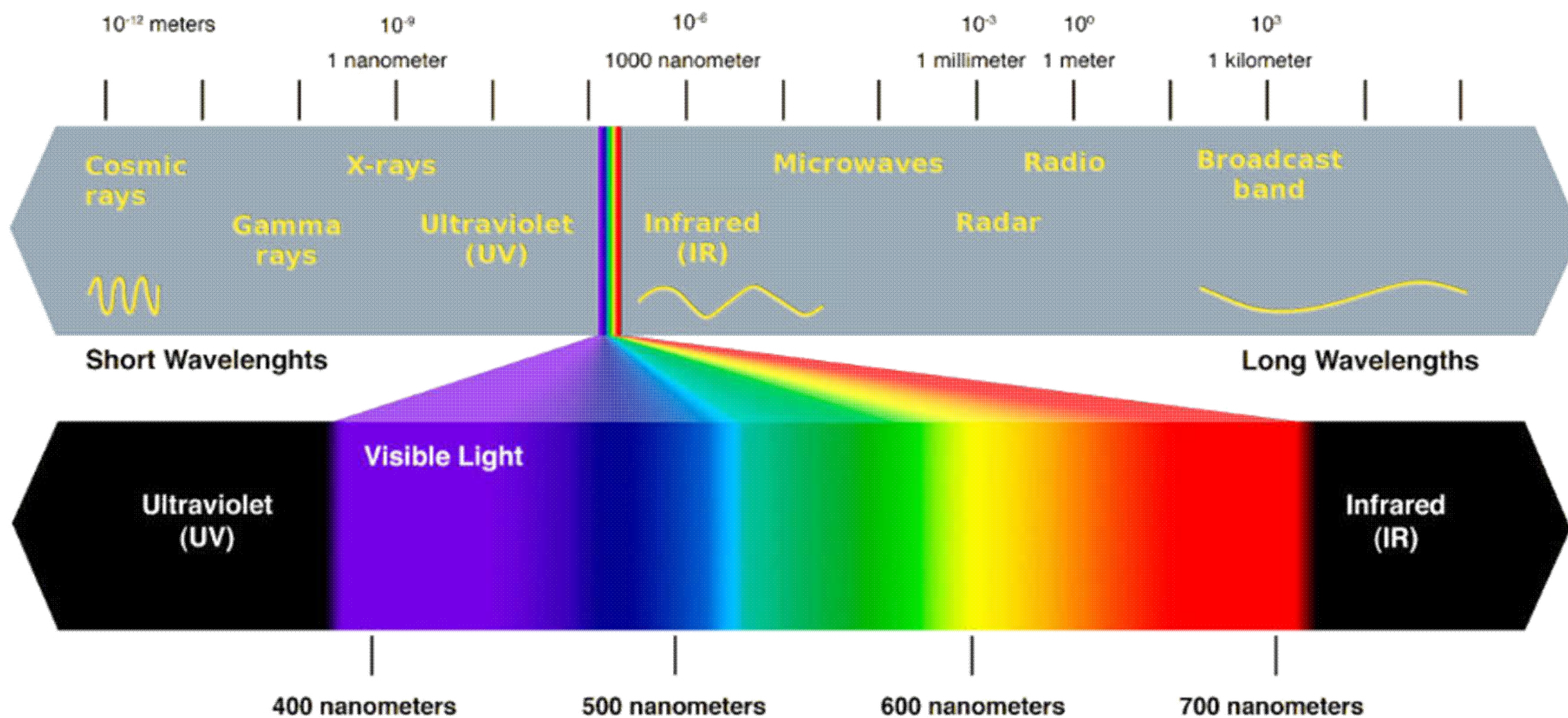
- elements, atoms, molecules, bonding, ...

# Table of Constants

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■ Free electron mass	$m_e = 9.11 \cdot 10^{-31} \text{ kg}$
■ Planck's constant	$h = 6.63 \cdot 10^{-34} \text{ J s}$
■ Reduced Planck's constant	$\hbar = h/2\pi = 1.05 \cdot 10^{-34} \text{ J s}$
■ Electron charge	$e = 1.6 \cdot 10^{-19} \text{ C}$
■ Energy	$1 \text{ eV} = 1.6 \cdot 10^{-19} \text{ J}$
■ Avogadro's number	$N_A = 6.02 \cdot 10^{23} \text{ /mol}$
■ Boltzmann constant	$k_B = 1.38 \cdot 10^{-23} \text{ J/K}$
■ Room temperature	$T = 300 \text{ K}$
■ Speed of light in vacuum	$c = 3 \cdot 10^8 \text{ m/s}$
■ Permittivity of vacuum	$\epsilon_0 = 8.85 \cdot 10^{-12} \text{ F/m}$
■ Permeability of vacuum	$\mu_0 = 4\pi \cdot 10^{-7} \text{ H/m}$

# Optics



**visible wavelength: 400–700 nm**

# Wave Functions

- Optical / Electromagnetic Wave
- Mechanical Wave
- Electron Wave
- ...



plane wave

$$F(x, t) = Ae^{i(kx - \omega t + \varphi)}$$

$A$  - amplitude

$k$  - wave vector ( $\text{m}^{-1}$ )

$\omega$  - angular frequency (Hz)

$\varphi$  - phase

$\nu$  - frequency (Hz)

$T$  - period (s)

$\lambda$  - wavelength (m)

$$\omega = 2\pi\nu$$

$$T = \frac{1}{\nu}$$

$$k = \frac{2\pi}{\lambda}$$

# Photons

- Photon Energy

$$E = \hbar\omega = h\nu = h\frac{c}{\lambda}$$

- Photon Momentum

$$p = \frac{E}{c} = \frac{h}{\lambda}$$

- Optical Wavelength

$$\lambda = \frac{hc}{E}$$



$$\lambda(\text{nm}) = \frac{1240}{E(\text{eV})}$$

$E$ (eV)	$\lambda$ (nm)
1	1240
2	620
3	413

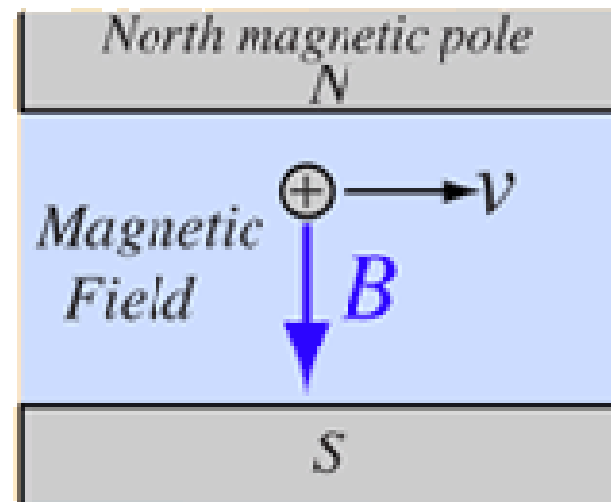
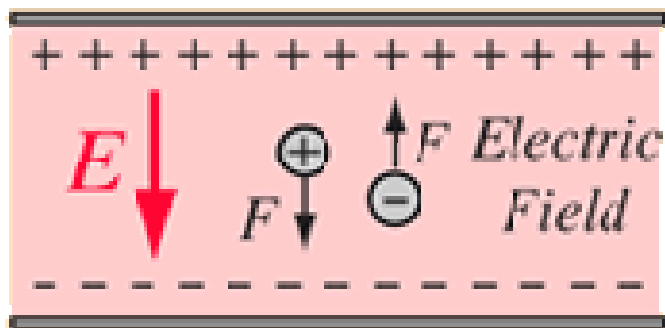
# Electrons in Electromagnetic Fields

- Lorentz force

$$\mathbf{F} = q\mathbf{E} + q\mathbf{v} \times \mathbf{B}$$

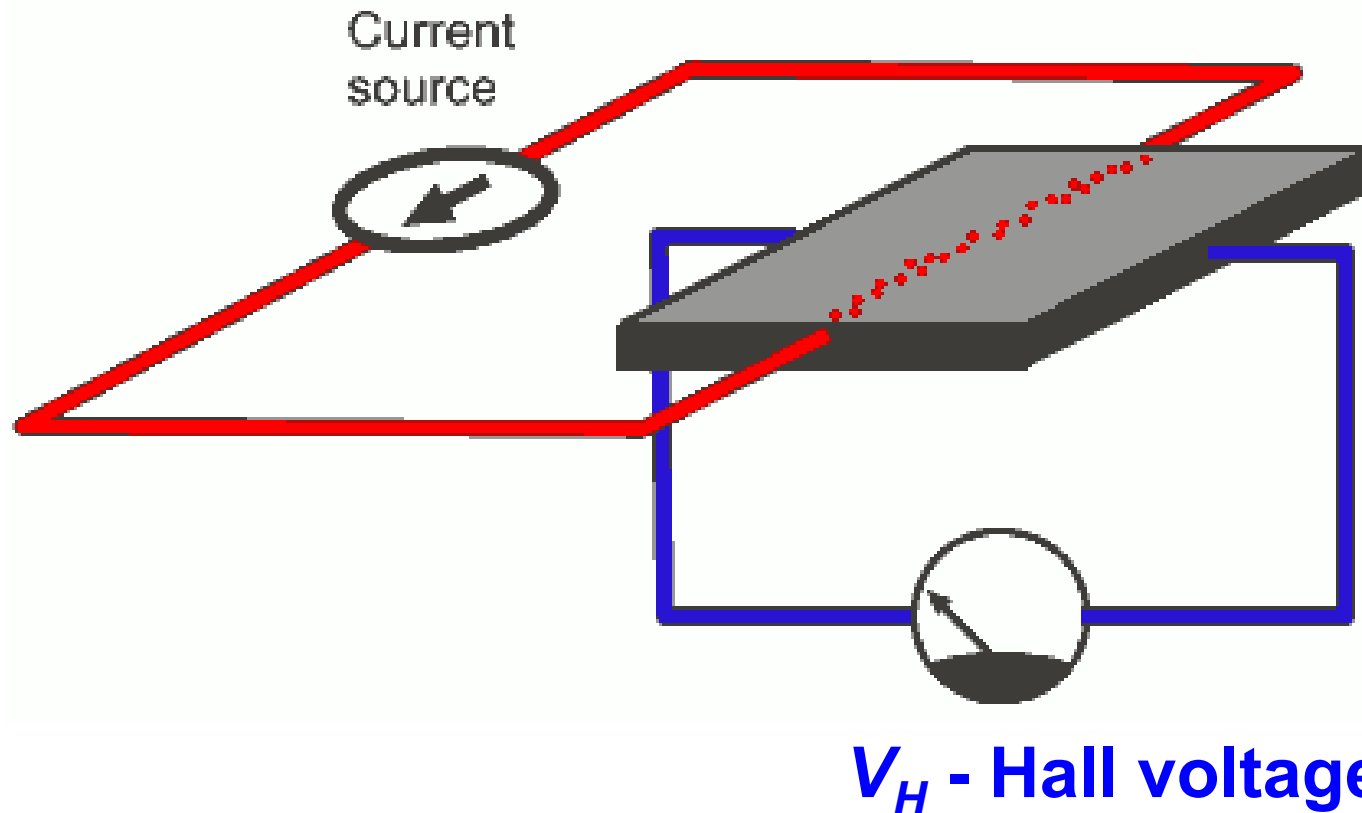
electric  
force

magnetic  
force



# Hall Effect 霍尔效应

- A current flows through a conductor
- $V_H$  is generated when applying  $B_z$

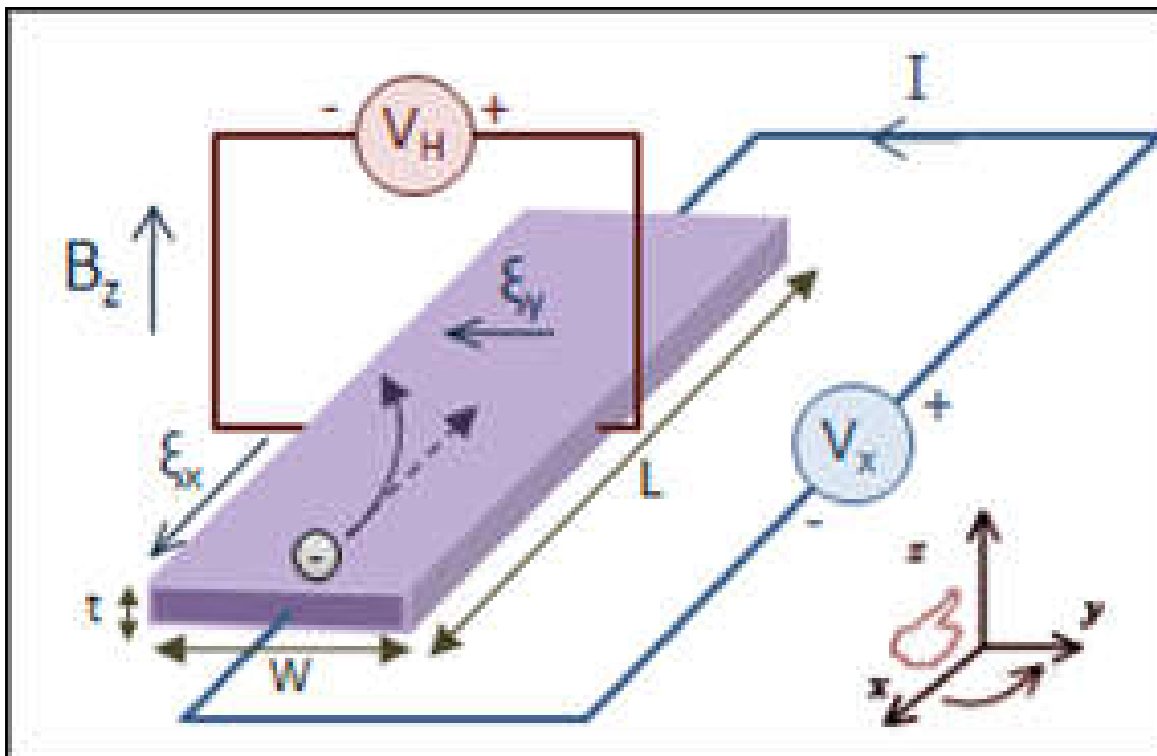




# Hall Effect 霍尔效应

- A current flows through a conductor
- $V_H$  is generated when applying  $B_z$

$$V_H = E_y \cdot w$$



$$E_y = R_H \cdot B_z \cdot j_x$$

$R_H$  - Hall coefficient

**By definition:**  
 positive charge:  $R_H > 0$   
 negative charge:  $R_H < 0$

# Quantum Mechanics

- Wave-Particle Duality 波粒二象性
- De Broglie Wave 德布罗意波 / 物质波

wavelength 波长

$$\lambda = \frac{h}{p}$$

wavenumber 波数  
wavevector 波矢

$$k = \frac{2\pi}{\lambda}$$

momentum 动量

$$p = mv = \hbar k$$

energy 能量

$$E = \frac{1}{2}mv^2 = \frac{p^2}{2m} = \frac{\hbar^2 k^2}{2m}$$

$$\hbar = \frac{h}{2\pi}$$

# Quantum Mechanics

- Wave function for electrons

$$\psi(\mathbf{r}, t)$$

$$|\psi|^2 = \psi^* \cdot \psi$$

probability at  $(\mathbf{r}, t)$

$$\psi(\mathbf{r}, t) = \psi(\mathbf{r}) \cdot \xi(t)$$

- Schrodinger Equation

$$\hat{H}\psi(\mathbf{r}, t) = E\psi(\mathbf{r}, t)$$

# Quantum Mechanics

- Schrodinger Equation (time dependent)

$$-i\hbar \frac{\partial}{\partial t} \psi(\mathbf{r}, t) = E\psi(\mathbf{r}, t) \quad \rightarrow \quad \xi(t) = \exp\left(-i \frac{E}{\hbar} t\right)$$

- Schrodinger Equation (time independent)

$$\hbar = \frac{h}{2\pi}$$

$$-\frac{\hbar^2}{2m} \nabla^2 \psi(\mathbf{r}, t) + V(\mathbf{r}) \cdot \psi(\mathbf{r}, t) = E\psi(\mathbf{r}, t)$$

$$\rightarrow -\frac{\hbar^2}{2m} \nabla^2 \psi(\mathbf{r}) + V(\mathbf{r}) \cdot \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

# Quantum Mechanics

- Free electrons

$$-\frac{\hbar^2}{2m} \nabla^2 \psi(\mathbf{r}) + V(\mathbf{r}) \cdot \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

free electron

$$V(\mathbf{r}) = 0$$



$$\nabla^2 \psi(\mathbf{r}) = -k^2 \psi(\mathbf{r})$$

$$k^2 = \frac{2mE}{\hbar^2}$$



$$\psi(\mathbf{r}) = \sum_{\mathbf{k}} A_{\mathbf{k}} \exp(i\mathbf{k} \cdot \mathbf{r})$$

$$\int_V \psi^* \cdot \psi d\mathbf{r} = 1$$

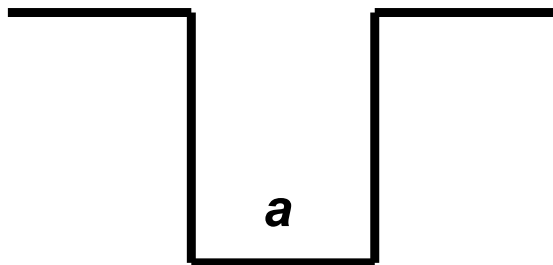
probability = 1

# Quantum Mechanics

- **Electron in a box (1D infinite well)**

$$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x) + V(x) \cdot \psi(x) = E\psi(x)$$

$$k^2 = \frac{2mE}{\hbar^2}$$



for  $0 < x < a$

$$\psi(x) = A \exp(ikx) + B \exp(-ikx)$$

and

$$\psi(x=0) = \psi(x=a) = 0$$

$$\int_0^a \psi(x) dx = 1$$

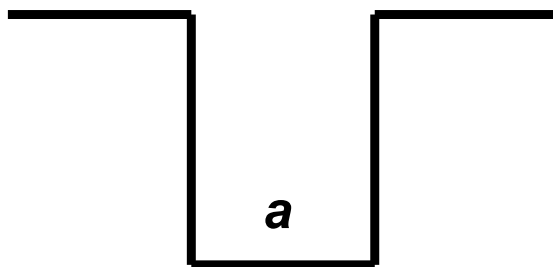
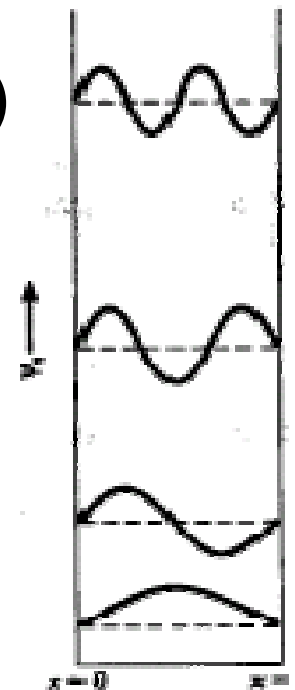
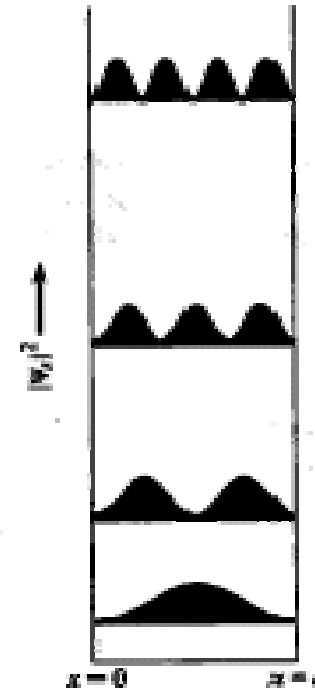
$$\begin{cases} V(x) = +\infty, & \text{when } x < 0 \\ V(x) = 0, & \text{when } 0 < x < a \\ V(x) = +\infty, & \text{when } x > a \end{cases}$$

# Quantum Mechanics

## ■ Electron in a box (1D infinite well)

$$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x) + V(x) \cdot \psi(x) = E\psi(x)$$

$$k^2 = \frac{2mE}{\hbar^2}$$


 $\psi(x)$ 

 $|\psi|^2$ 


$$\begin{cases} V(x) = +\infty, & \text{when } x < 0 \\ V(x) = 0, & \text{when } 0 < x < a \\ V(x) = +\infty, & \text{when } x > a \end{cases}$$

# Quantum Mechanics

## 1D Harmonic Oscillator

$$-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x) + V(x) \cdot \psi(x) = E\psi(x)$$

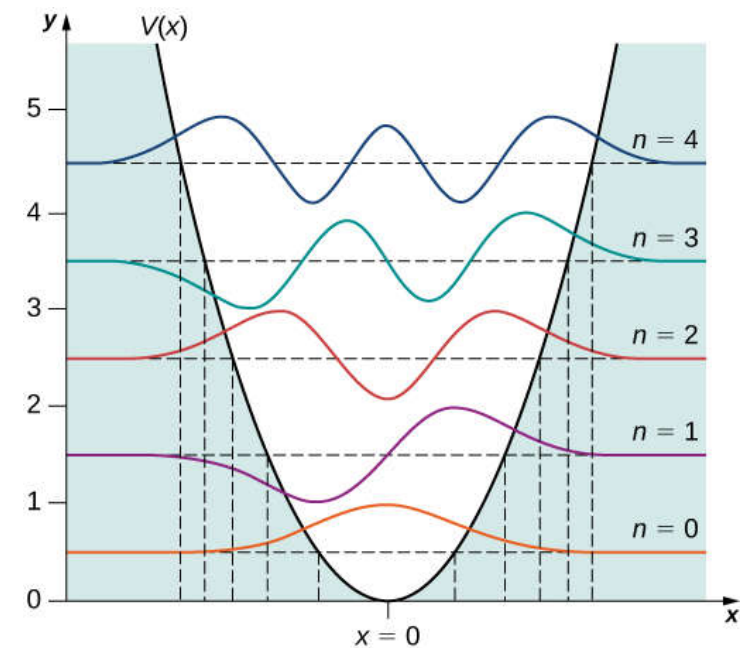
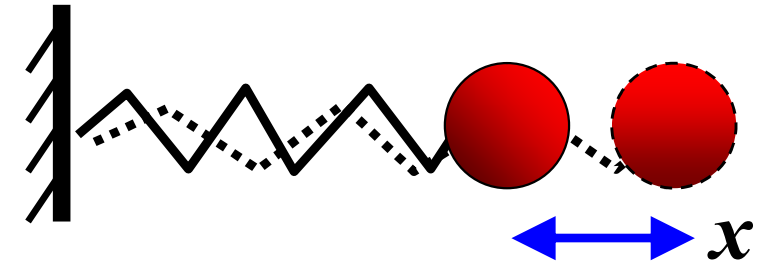
$$V(x) = \frac{1}{2} Kx^2 = \frac{1}{2} m\omega^2 x^2$$

$$\omega = \sqrt{\frac{K}{m}}$$

$$\rightarrow E_n = \left( \frac{1}{2} + n \right) \hbar\omega \quad n = 0, 1, 2, \dots$$

$$\psi_n(x) = e^{-\beta x^2/2} \cdot H_n(x)$$

$$\beta = \frac{\sqrt{Km}}{\hbar}$$



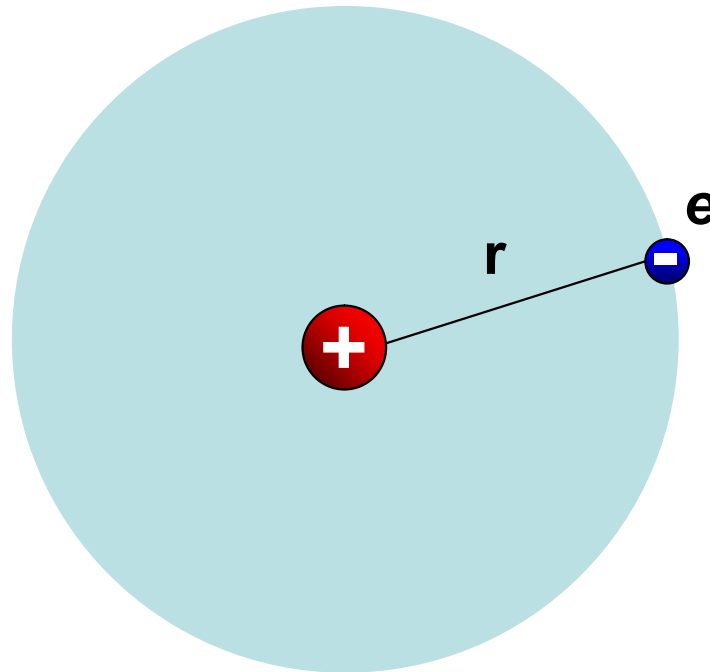
$H_n(x)$   
Hermite polynomial 17



# Quantum Mechanics

- Hydrogen atom

$$V(\mathbf{r}) = -\frac{e^2}{4\pi\epsilon_0} \frac{1}{r}$$



# Quantum Mechanics

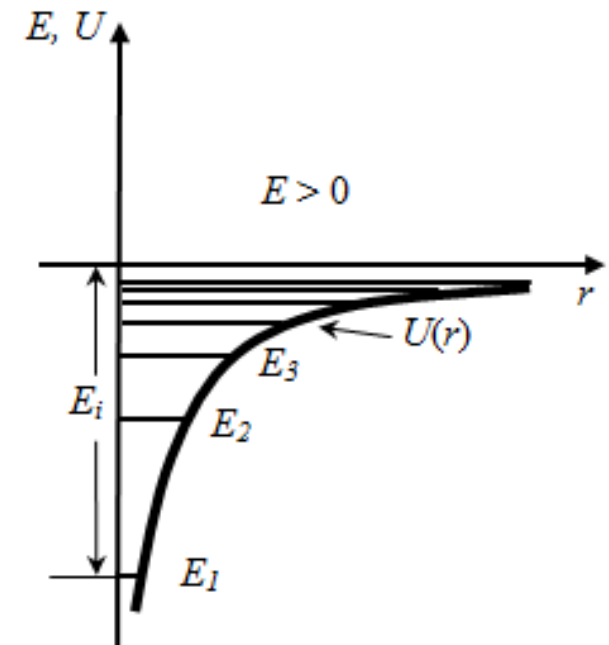
- Hydrogen atom

$$V(\mathbf{r}) = -\frac{e^2}{4\pi\epsilon_0} \frac{1}{r}$$

$$-\frac{\hbar^2}{2m} \nabla^2 \psi(\mathbf{r}) + V(\mathbf{r}) \cdot \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

→ 
$$\psi(r, \theta, \varphi) = R_{nl}(r) \cdot Y_{lm}(\theta, \varphi)$$

$$E_n = -\frac{me^4}{8\epsilon_0^2 h^2 n^2} = -\frac{13.6 \text{ eV}}{n^2}$$

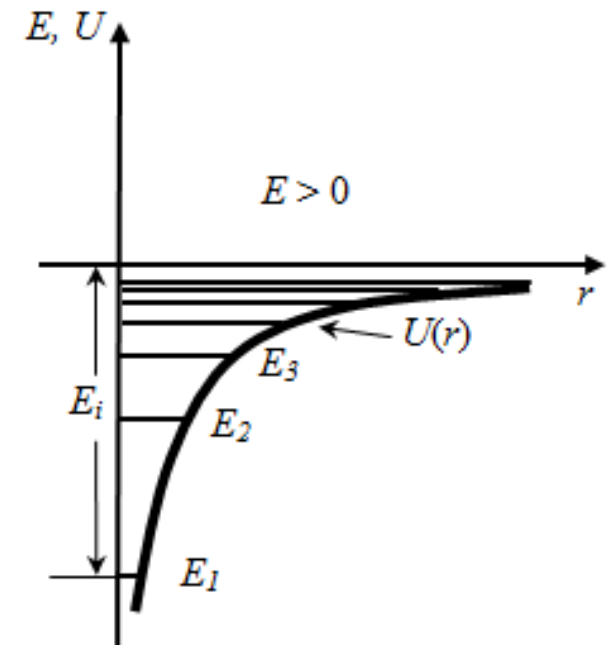
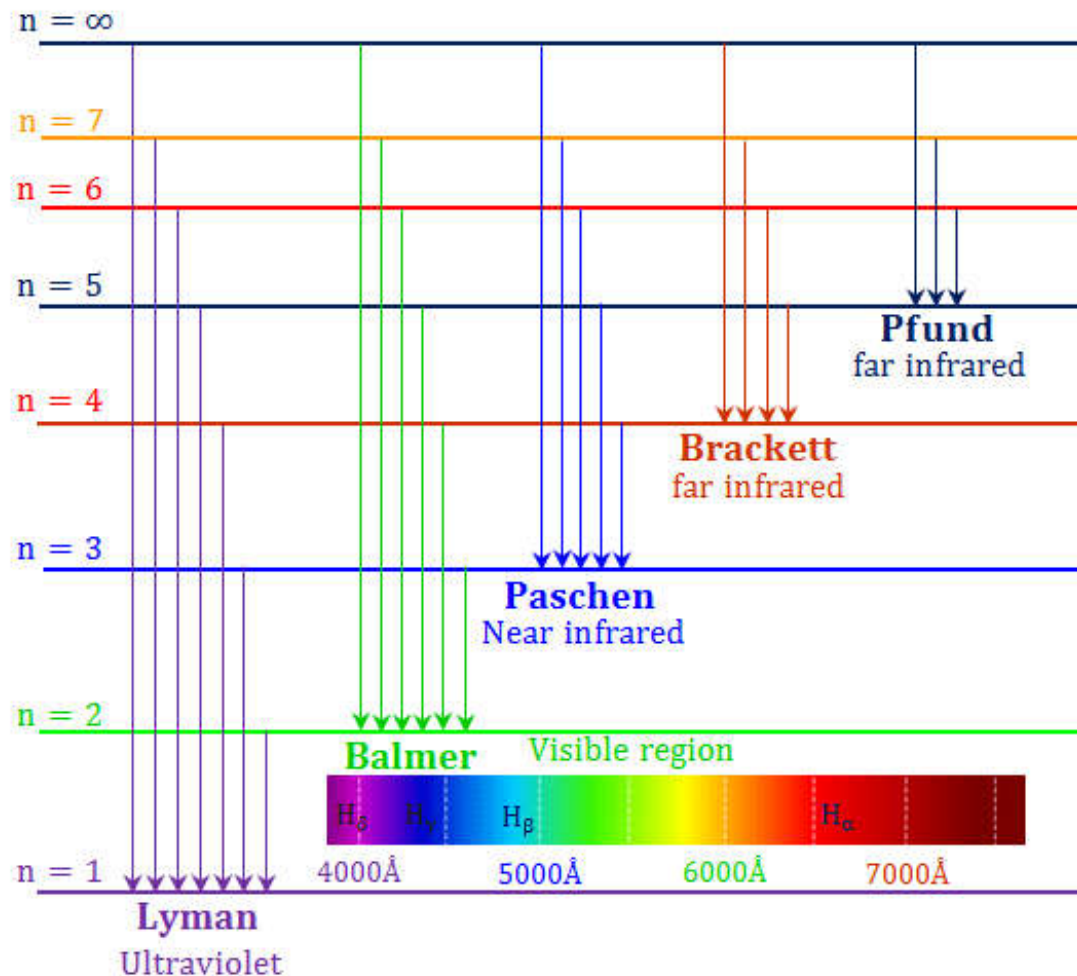


$n, l, m$  - quantum numbers  
 $m_s$  - spin (+1/2, -1/2)

# Quantum Mechanics

## Hydrogen atom

$$E_n = -\frac{13.6 \text{ eV}}{n^2}$$



Emissions of atoms have discrete energy lines

# Atoms with Many Electrons

- Quantum Numbers  $n, l, m, m_s$ 
  - Principal:  $n = 1, 2, 3, 4, \dots$
  - Angular momentum:  $l = 0, 1, 2, 3, \dots (n-1)$
  - Magnetic:  $m = -l, \dots, -1, 0, +1, \dots +l$
  - Spin:  $m_s = +1/2, -1/2$

$$\psi(r, \theta, \varphi) = R_{nl}(r) \cdot Y_{lm}(\theta, \varphi)$$

# Atoms with Many Electrons

## Quantum Numbers $n, l, m, m_s$

	$s (\ell = 0)$	$p (\ell = 1)$			$d (\ell = 2)$					$f (\ell = 3)$							
	$m = 0$	$m = 0$	$m = \pm 1$		$m = 0$	$m = \pm 1$		$m = \pm 2$		$m = 0$	$m = \pm 1$		$m = \pm 2$		$m = \pm 3$		
	$s$	$p_z$	$p_x$	$p_y$	$d_{z^2}$	$d_{xx}$	$d_{yz}$	$d_{xy}$	$d_{x^2-y^2}$	$f_{z^2}$	$f_{xz^2}$	$f_{yz^2}$	$f_{xyz}$	$f_{z(x^2-y^2)}$	$f_{x(x^2-3y^2)}$	$f_{y(3x^2-y^2)}$	
$n = 1$																	
$n = 2$																	
$n = 3$																	
$n = 4$																	
$n = 5$										...	...	...	...	...	...	...	...
$n = 6$					...	...	...	...	...	...	...	...	...	...	...	...	...
$n = 7$		...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...

# Quantum Mechanics

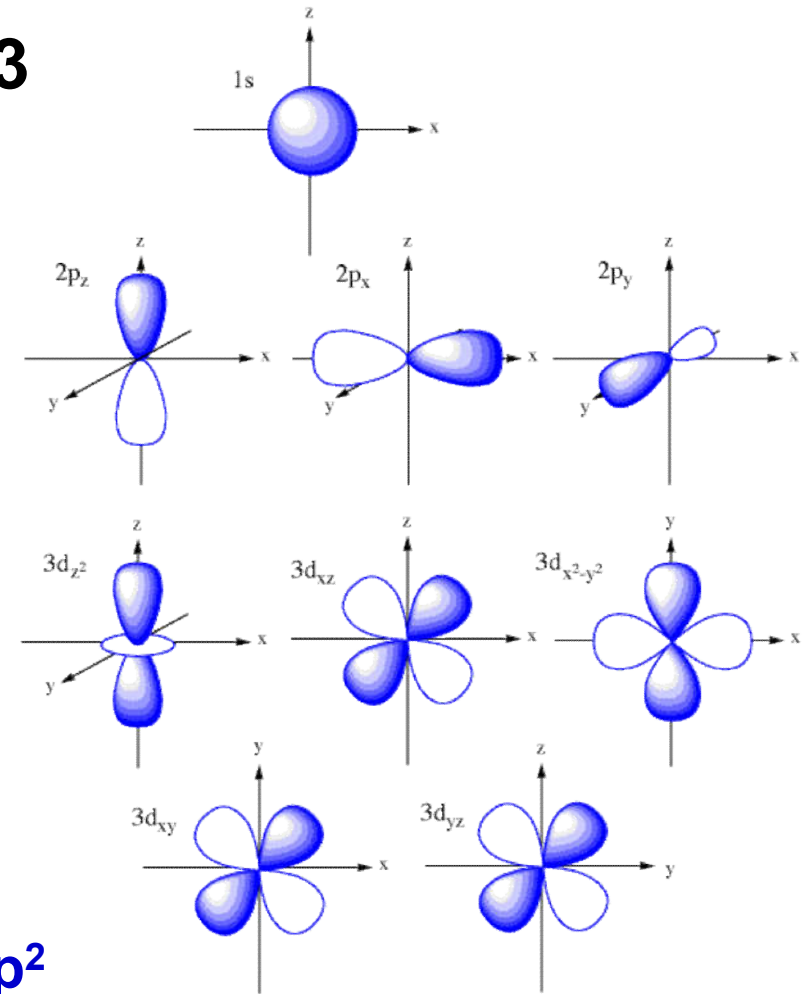
- Angular momentum:  $l = 0, 1, 2, 3$
- Atomic orbitals: s p d f

- **Examples**

- Hydrogen (H)  $1s^1$
- Helium (He)  $1s^2$
- Lithium (Li)  $[1s^2] 2s^1$
- Carbon (C)  $[1s^2] 2s^2 2p^2$
- Neon (Ne)  $[1s^2] 2s^2 2p^6$
- Sodium (Na)  $[1s^2 2s^2 2p^6] 3s^1$
- Silicon (Si)  $[1s^2 2s^2 2p^6] 3s^2 3p^2$

**core electrons**

**valence electrons**



## Electron Configurations in the Periodic Table

1 <b>H</b> 1s																	2 <b>He</b> 1s																												
3 <b>Li</b> 2s	4 <b>Be</b>																	5 <b>B</b>	6 <b>C</b>	7 <b>N</b>	8 <b>O</b>	9 <b>F</b>	10 <b>Ne</b>																						
11 <b>Na</b> 3s	12 <b>Mg</b>																	13 <b>Al</b>	14 <b>Si</b>	15 <b>P</b>	16 <b>S</b>	17 <b>Cl</b>	18 <b>Ar</b>																						
19 <b>K</b> 4s	20 <b>Ca</b>	21 <b>Sc</b>	22 <b>Ti</b>	23 <b>V</b>	24 <b>Cr</b>	25 <b>Mn</b>	26 <b>Fe</b>	27 <b>Co</b>	28 <b>Ni</b>	29 <b>Cu</b>	30 <b>Zn</b>	31 <b>Ga</b>	32 <b>Ge</b>	33 <b>As</b>	34 <b>Se</b>	35 <b>Br</b>	36 <b>Kr</b>																												
37 <b>Rb</b> 5s	38 <b>Sr</b>	39 <b>Y</b>	40 <b>Zr</b>	41 <b>Nb</b>	42 <b>Mo</b>	43 <b>Tc</b>	44 <b>Ru</b>	45 <b>Rh</b>	46 <b>Pd</b>	47 <b>Ag</b>	48 <b>Cd</b>	49 <b>In</b>	50 <b>Sn</b>	51 <b>Sb</b>	52 <b>Te</b>	53 <b>I</b>	54 <b>Xe</b>																												
55 <b>Cs</b> 6s	56 <b>Ba</b>	57 <b>La</b>	72 <b>Hf</b>	73 <b>Ta</b>	74 <b>W</b>	75 <b>Re</b>	76 <b>Os</b>	77 <b>Ir</b>	78 <b>Pt</b>	79 <b>Au</b>	80 <b>Hg</b>	81 <b>Tl</b>	82 <b>Pb</b>	83 <b>Bi</b>	84 <b>Po</b>	85 <b>At</b>	86 <b>Rn</b>																												
87 <b>Fr</b> 7s	88 <b>Ra</b>	89 <b>Ac</b>	104 <b>Rf</b>	105 <b>Db</b>	106 <b>Sg</b>	107 <b>Bh</b>	108 <b>Hs</b>	109 <b>Mt</b>	110	111	112	113	114																																
		<table border="1"> <tbody> <tr> <td>58 <b>Ce</b></td> <td>59 <b>Pr</b></td> <td>60 <b>Nd</b></td> <td>61 <b>Pm</b></td> <td>62 <b>Sm</b></td> <td>63 <b>Eu</b></td> <td>64 <b>Gd</b></td> <td>65 <b>Tb</b></td> <td>66 <b>Dy</b></td> <td>67 <b>Ho</b></td> <td>68 <b>Er</b></td> <td>69 <b>Tm</b></td> <td>70 <b>Yb</b></td> <td>71 <b>Lu</b></td> </tr> <tr> <td>90 <b>Th</b></td> <td>91 <b>Pa</b></td> <td>92 <b>U</b></td> <td>93 <b>Np</b></td> <td>94 <b>Pu</b></td> <td>95 <b>Am</b></td> <td>96 <b>Cm</b></td> <td>97 <b>Bk</b></td> <td>98 <b>Cf</b></td> <td>99 <b>Es</b></td> <td>100 <b>Fm</b></td> <td>101 <b>Md</b></td> <td>102 <b>No</b></td> <td>103 <b>Lr</b></td> </tr> </tbody> </table>																58 <b>Ce</b>	59 <b>Pr</b>	60 <b>Nd</b>	61 <b>Pm</b>	62 <b>Sm</b>	63 <b>Eu</b>	64 <b>Gd</b>	65 <b>Tb</b>	66 <b>Dy</b>	67 <b>Ho</b>	68 <b>Er</b>	69 <b>Tm</b>	70 <b>Yb</b>	71 <b>Lu</b>	90 <b>Th</b>	91 <b>Pa</b>	92 <b>U</b>	93 <b>Np</b>	94 <b>Pu</b>	95 <b>Am</b>	96 <b>Cm</b>	97 <b>Bk</b>	98 <b>Cf</b>	99 <b>Es</b>	100 <b>Fm</b>	101 <b>Md</b>	102 <b>No</b>	103 <b>Lr</b>
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by: Sarah Faizi

# Statistical Mechanics

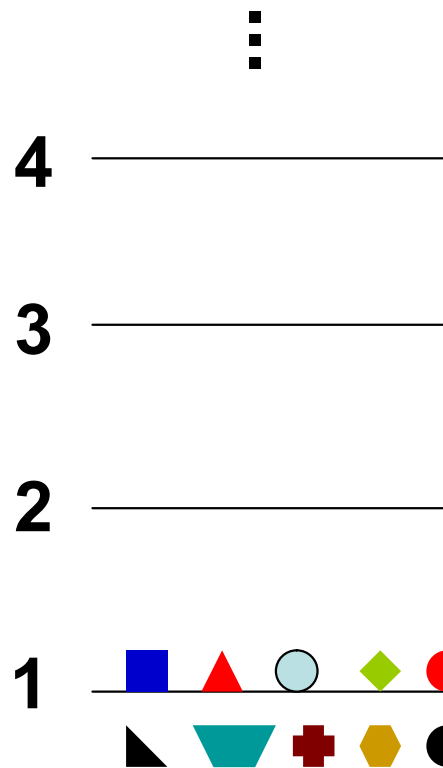
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- **Maxwell–Boltzmann Distribution 玻尔兹曼分布**
  - distinguishable, non-interaction particles: ideal gas, ...
- **Bose–Einstein Distribution 玻色-爱因斯坦分布**
  - indistinguishable particles
  - Bosons: photons, phonons, ...
  - integer spin
- **Fermi–Dirac Distribution 费米-狄拉克分布**
  - indistinguishable particles
  - Fermions: electrons, ...
  - half-integer spin
  - Pauli exclusion principle (泡利不相容原理)

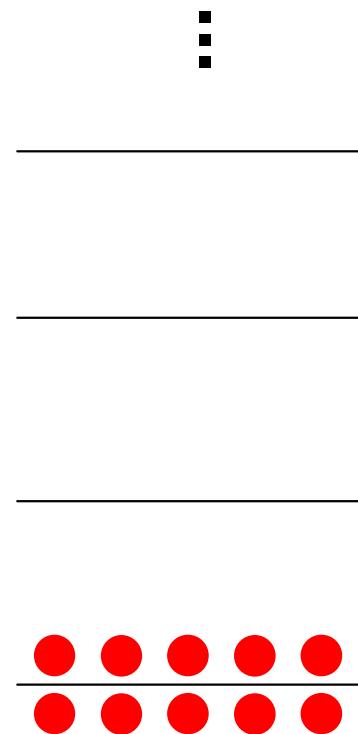


# Statistical Mechanics

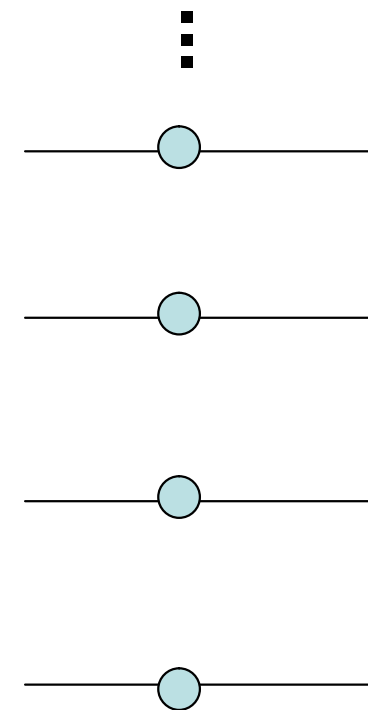
- At  $T = 0$  K



Maxwell-Boltzmann



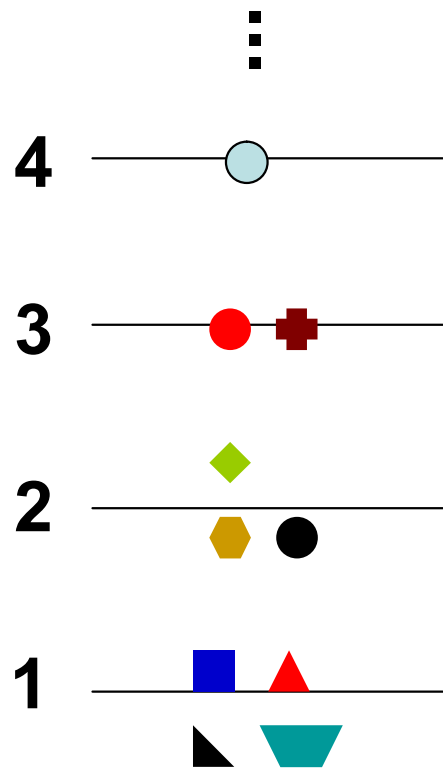
Bose-Einstein



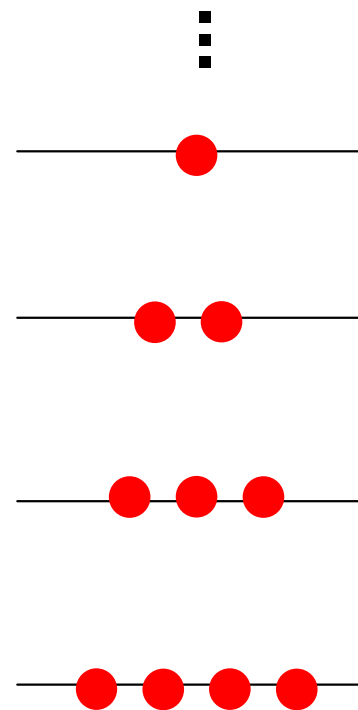
Fermi-Dirac

# Statistical Mechanics

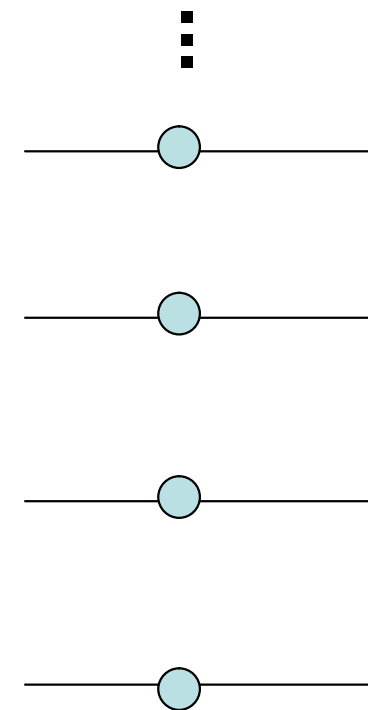
- At  $T > 0$  K



Maxwell-Boltzmann



Bose-Einstein



Fermi-Dirac

# Statistical Mechanics

## ■ Fermi–Dirac Distribution

- Fermions: electrons, ...

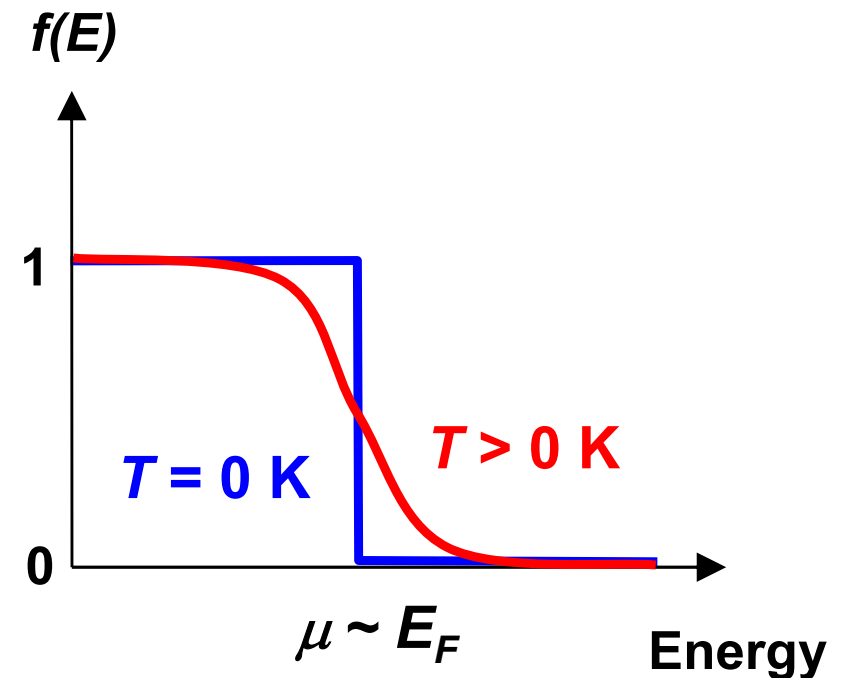
$$f(E) = \frac{1}{e^{(E-\mu)/k_B T} + 1}$$

$f(E)$  - probability that an energy state  $E$  is occupied

$\mu$  - chemical potential

$E_F$  - Fermi energy

$\mu = E_F$  when  $T = 0$  K



At  $T = 0$  K

$f(E) = 1$  for  $E < \mu$

$f(E) = 0$  for  $E > \mu$

# Chemistry

**Periodic Table of the Elements**

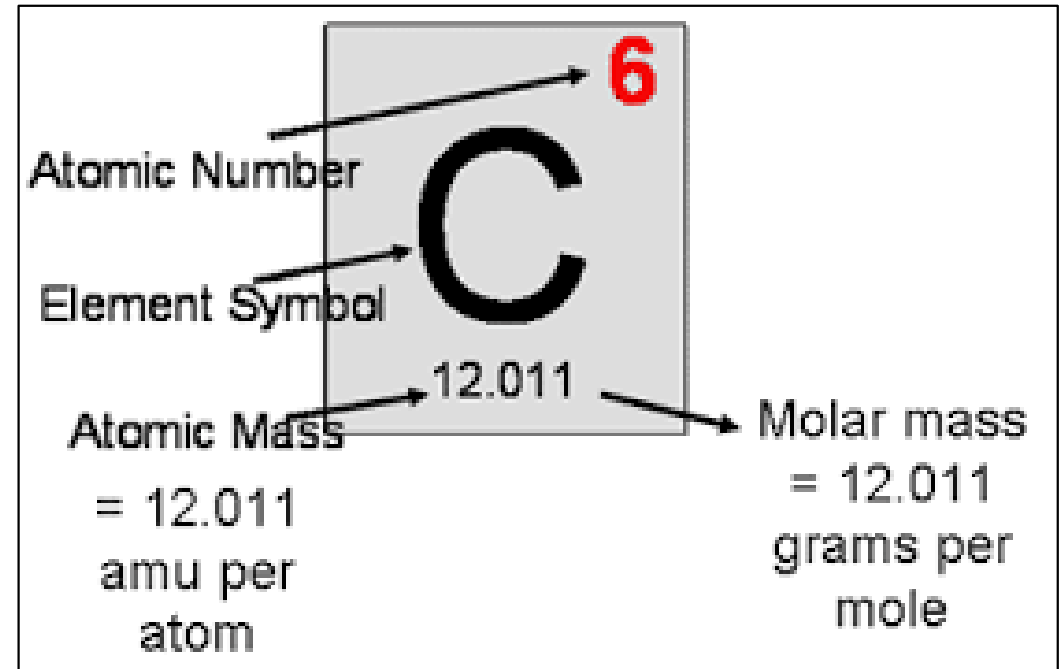
1 IA 1A												13 IIIA 3A		14 IVA 4A	15 VA 5A	16 VIA 6A	17 VIIA 7A	18 VIIIA 8A	
1 <b>H</b> Hydrogen 1.008												5 <b>B</b> Boron 10.811	6 <b>C</b> Carbon 12.011	7 <b>N</b> Nitrogen 14.007	8 <b>O</b> Oxygen 15.999	9 <b>F</b> Fluorine 18.998	10 <b>Ne</b> Neon 20.180		
3 <b>Li</b> Lithium 6.941	4 <b>Be</b> Beryllium 9.012											13 <b>Al</b> Aluminum 26.982	14 <b>Si</b> Silicon 28.086	15 <b>P</b> Phosphorus 30.974	16 <b>S</b> Sulfur 32.066	17 <b>Cl</b> Chlorine 35.453	18 <b>Ar</b> Argon 39.948		
11 <b>Na</b> Sodium 22.990	12 <b>Mg</b> Magnesium 24.305	3 IIIB 3B	4 IVB 4B	5 VB 5B	6 VIB 6B	7 VIIB 7B	8 VIII 8		9 VIII 8	10 VIII 8	11 IB 1B	12 IIB 2B	31 <b>Ga</b> Gallium 69.723	32 <b>Ge</b> Germanium 72.631	33 <b>As</b> Arsenic 74.922	34 <b>Se</b> Selenium 78.971	35 <b>Br</b> Bromine 79.904	36 <b>Kr</b> Krypton 84.798	
19 <b>K</b> Potassium 39.098	20 <b>Ca</b> Calcium 40.078	21 <b>Sc</b> Scandium 44.956	22 <b>Ti</b> Titanium 47.867	23 <b>V</b> Vanadium 50.942	24 <b>Cr</b> Chromium 51.996	25 <b>Mn</b> Manganese 54.938	26 <b>Fe</b> Iron 55.845	27 <b>Co</b> Cobalt 58.933	28 <b>Ni</b> Nickel 58.693	29 <b>Cu</b> Copper 63.546	30 <b>Zn</b> Zinc 65.38	31 <b>Ga</b> Gallium 69.723	32 <b>Ge</b> Germanium 72.631	33 <b>As</b> Arsenic 74.922	34 <b>Se</b> Selenium 78.971	35 <b>Br</b> Bromine 79.904	36 <b>Kr</b> Krypton 84.798		
37 <b>Rb</b> Rubidium 84.468	38 <b>Sr</b> Strontium 87.62	39 <b>Y</b> Yttrium 88.906	40 <b>Zr</b> Zirconium 91.224	41 <b>Nb</b> Niobium 92.906	42 <b>Mo</b> Molybdenum 95.95	43 <b>Tc</b> Technetium 98.907	44 <b>Ru</b> Ruthenium 101.07	45 <b>Rh</b> Rhodium 102.906	46 <b>Pd</b> Palladium 106.42	47 <b>Ag</b> Silver 107.868	48 <b>Cd</b> Cadmium 112.411	49 <b>In</b> Indium 114.818	50 <b>Sn</b> Tin 118.711	51 <b>Sb</b> Antimony 121.760	52 <b>Te</b> Tellurium 127.6	53 <b>I</b> Iodine 126.904	54 <b>Xe</b> Xenon 131.294		
55 <b>Cs</b> Cesium 132.905	56 <b>Ba</b> Barium 137.328	57-71	72 <b>Hf</b> Hafnium 178.49	73 <b>Ta</b> Tantalum 180.948	74 <b>W</b> Tungsten 183.84	75 <b>Re</b> Rhenium 186.207	76 <b>Os</b> Osmium 190.23	77 <b>Ir</b> Iridium 192.217	78 <b>Pt</b> Platinum 195.085	79 <b>Au</b> Gold 196.967	80 <b>Hg</b> Mercury 200.592	81 <b>Tl</b> Thallium 204.383	82 <b>Pb</b> Lead 207.2	83 <b>Bi</b> Bismuth 208.980	84 <b>Po</b> Polonium [208.982]	85 <b>At</b> Astatine 209.987	86 <b>Rn</b> Radon 222.018		
87 <b>Fr</b> Francium 223.020	88 <b>Ra</b> Radium 226.025	89-103	104 <b>Rf</b> Rutherfordium [261]	105 <b>Db</b> Dubnium [262]	106 <b>Sg</b> Seaborgium [266]	107 <b>Bh</b> Bohrium [264]	108 <b>Hs</b> Hassium [269]	109 <b>Mt</b> Meitnerium [268]	110 <b>Ds</b> Darmstadtium [269]	111 <b>Rg</b> Roentgenium [272]	112 <b>Cn</b> Copernicium [277]	113 <b>Uut</b> Ununtrium unknown	114 <b>Fl</b> Flerovium [289]	115 <b>Uup</b> Ununpentium unknown	116 <b>Lv</b> Livermorium [298]	117 <b>Uus</b> Ununseptium unknown	118 <b>Uuo</b> Ununoctium unknown		

Lanthanide Series	57 <b>La</b> Lanthanum 138.905	58 <b>Ce</b> Cerium 140.116	59 <b>Pr</b> Praseodymium 140.908	60 <b>Nd</b> Neodymium 144.243	61 <b>Pm</b> Promethium 144.913	62 <b>Sm</b> Samarium 150.36	63 <b>Eu</b> Europium 151.964	64 <b>Gd</b> Gadolinium 157.25	65 <b>Tb</b> Terbium 158.925	66 <b>Dy</b> Dysprosium 162.500	67 <b>Ho</b> Holmium 164.930	68 <b>Er</b> Erbium 167.259	69 <b>Tm</b> Thulium 168.934	70 <b>Yb</b> Ytterbium 173.055	71 <b>Lu</b> Lutetium 174.967
Actinide Series	89 <b>Ac</b> Actinium 227.028	90 <b>Th</b> Thorium 232.038	91 <b>Pa</b> Protactinium 231.036	92 <b>U</b> Uranium 238.029	93 <b>Np</b> Neptunium 237.048	94 <b>Pu</b> Plutonium 244.064	95 <b>Am</b> Americium 243.061	96 <b>Cm</b> Curium 247.070	97 <b>Bk</b> Berkelium 247.070	98 <b>Cf</b> Californium 251.080	99 <b>Es</b> Einsteinium [254]	100 <b>Fm</b> Fermium 257.095	101 <b>Md</b> Mendelevium 258.1	102 <b>No</b> Nobelium 259.101	103 <b>Lr</b> Lawrencium [262]

Alkali Metal	Alkaline Earth	Transition Metal	Basic Metal	Semimetal	Nonmetal	Halogen	Noble Gas	Lanthanide	Actinide
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# Chemistry

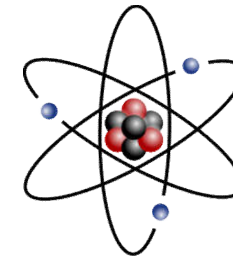
- Periodic Table
- Atomic number
- Mass number
  - amu / atom
  - g / mol
- Avogadro's number  $N_A$ 
  - $1 \text{ mol} = 6.022 * 10^{23}$



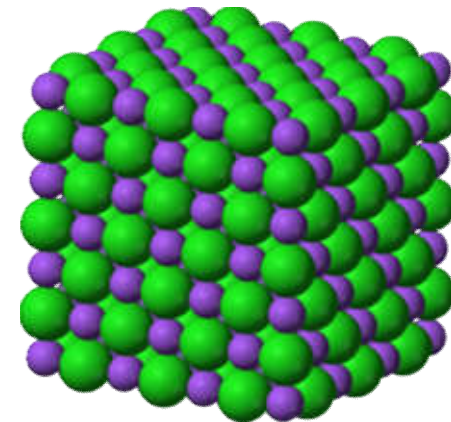
# Chemical Bonding 化学键

## ■ Solids are formed by chemical bonding between atoms

- Metallic Bonding 金属键
- Ionic Bonding 离子键
- Covalent Bonding 共价键
- Van der Waals Bonding 范德华键
- Hydrogen Bonding 氢键
- ...



atom



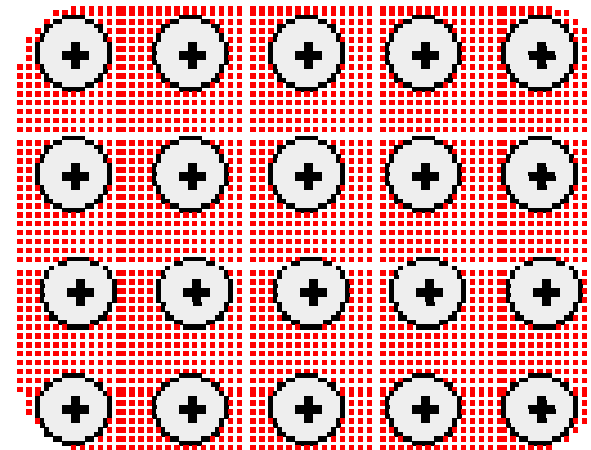
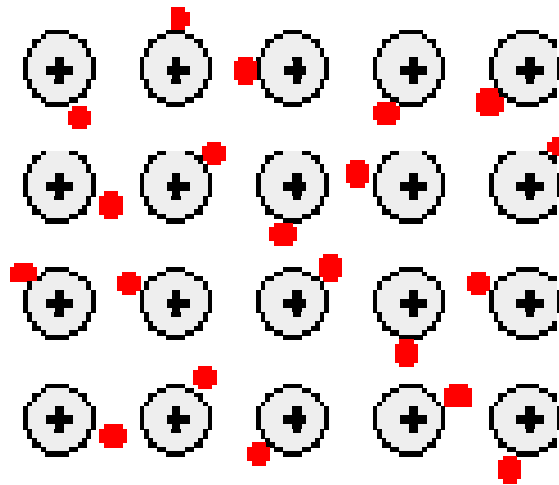
solid

## ■ Valence electrons form bonds

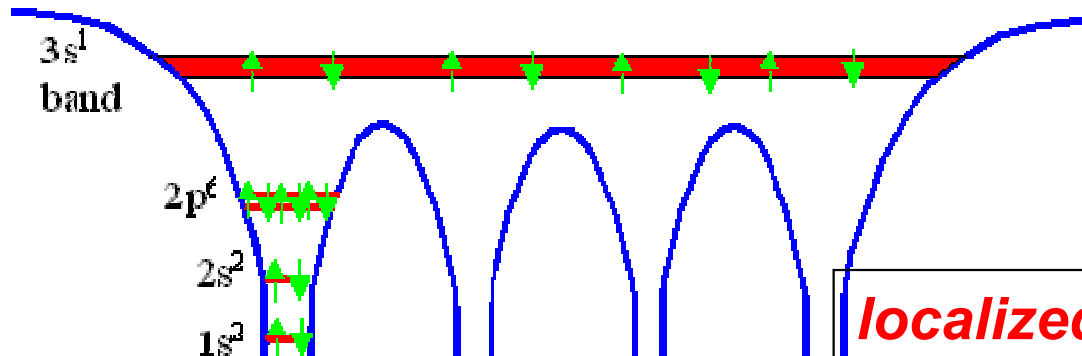
- Silicon (Si)       $[1s^2 2s^2 2p^6] \underline{3s^2 3p^2}$

# Metallic Bonding 金属键

- Positive metal ions in a sea of delocalised electrons



delocalised electrons



Sodium (Na)  $[1s^2 2s^2 2p^6] 3s^1$

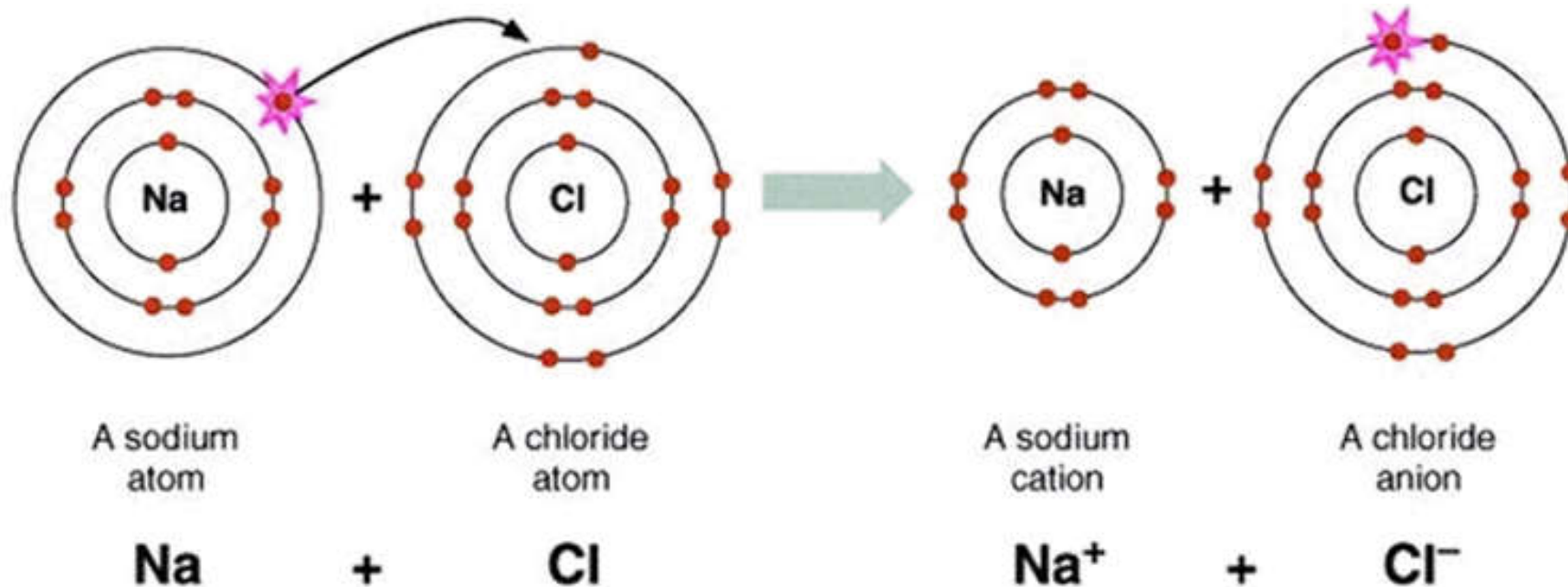
*localized electron*  
(core electron)

*'delocalized' electron*  
(free electron)

# Ionic Bonding 离子键

## ■ NaCl

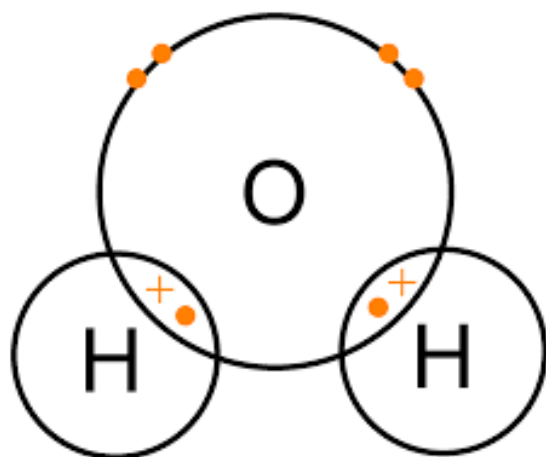
- Na loses an electron  $\longrightarrow$   $\text{Na}^+$  (cation)
- Cl gains an electron  $\longrightarrow$   $\text{Cl}^-$  (anion)
- Cations and anions are held by electrostatic attractions



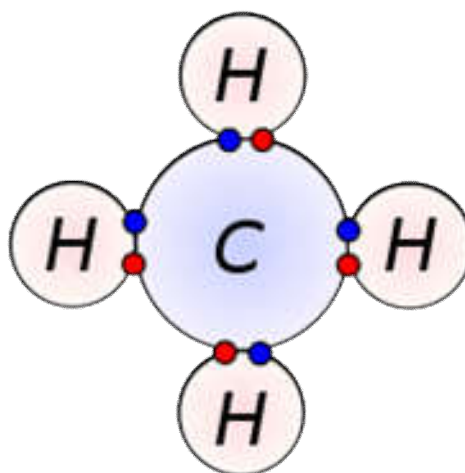


# Covalent Bonding 共价键

- Electron pairs are shared between atoms

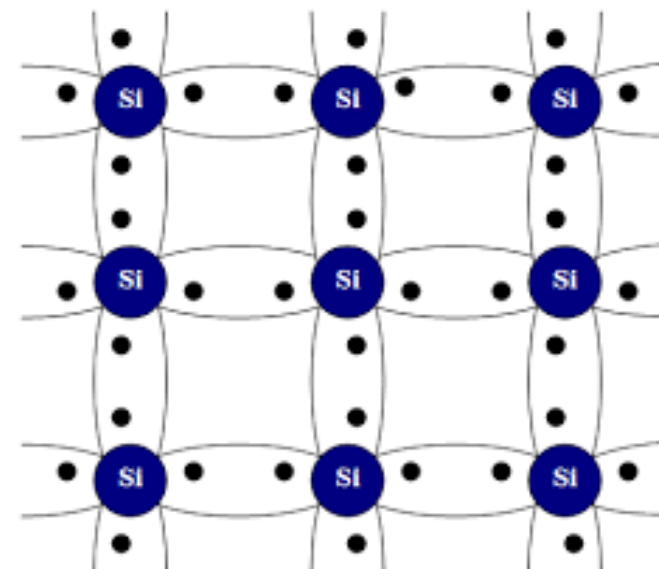


$\text{H}_2\text{O}$



● Electron from hydrogen  
● Electron from carbon

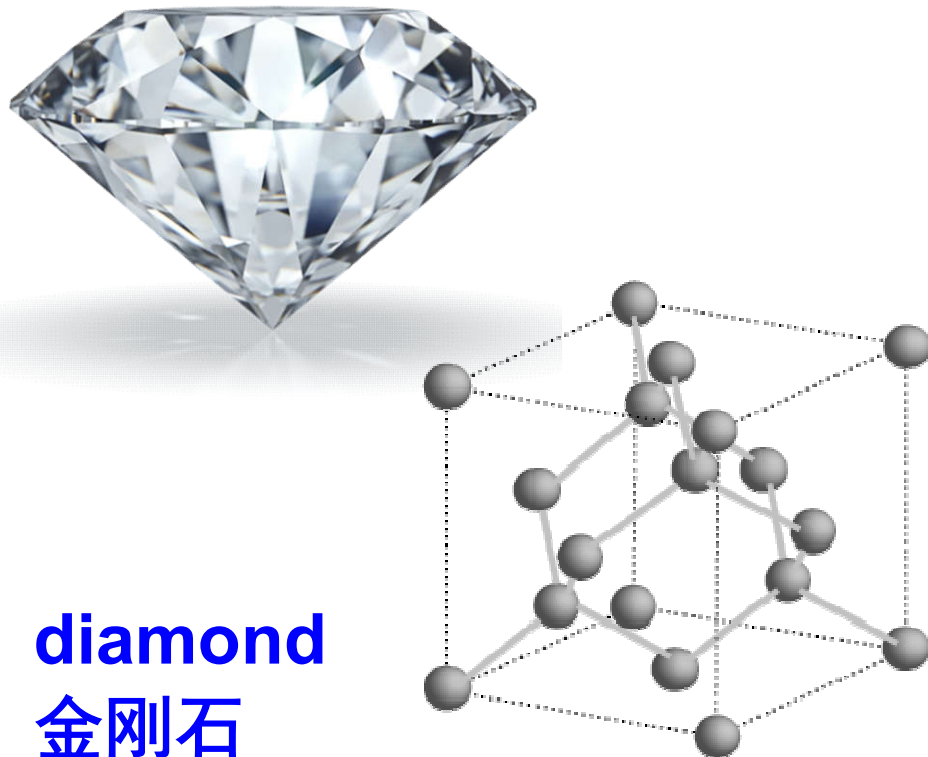
$\text{CH}_4$



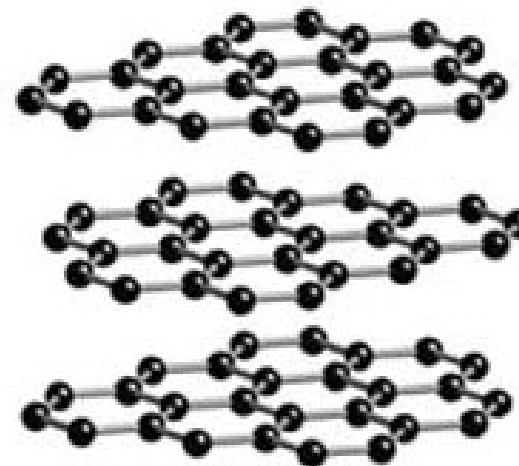
Silicon

# Example: Carbon

- **Diamond is the hardest material and an insulator**
  - **all the 4 valence electrons form covalent bonds**



- **Graphite is the softest solid and a conductor**
  - **atoms in each plane form covalent bonds (3 electrons)**
  - **There is one free electron**
  - **stacking layers form metallic bonds**



**graphite**  
石墨

# Electronegativity (EN) 电负性

- Tendency of an atom to attract a bonding pair of electrons
  - $EN(\text{Li}) = 1.0$        $EN(\text{F}) = 4.0$
- A-B bond usually has mixed bonding properties
  - similar EN       $\longrightarrow$       more covalent bonding
  - different EN       $\longrightarrow$       more ionic bonding

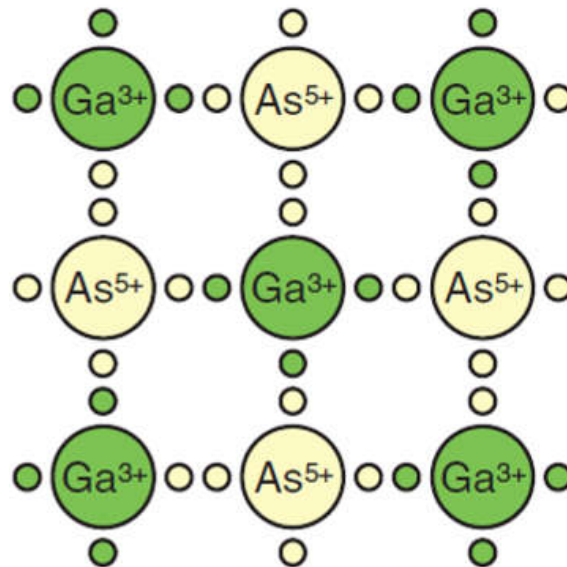
H 2.1																			He
Li 1.0	Be 1.5											B 2.0	C 2.5	N 3.0	O 3.5	F 4.0			Ne
Na 0.9	Mg 1.2											Al 1.5	Si 1.8	P 2.1	S 2.5	Cl 3.0			Ar
K 0.8	Ca 1.0	Sc 1.3	Ti 1.5	V 1.6	Cr 1.6	Mn 1.5	Fe 1.8	Co 1.9	Ni 1.8	Cu 1.9	Zn 1.6	Ga 1.6	Ge 1.8	As 2.0	Se 2.4	Br 2.8			Kr
Rb 0.8	Sr 1.0	Y 1.2	Zr 1.4	Nb 1.6	Mo 1.8	Tc 1.9	Ru 2.2	Rh 2.2	Pd 2.2	Ag 1.9	Cd 1.7	In 1.7	Sn 1.8	Sb 1.9	Te 2.1	I 2.5			Xe
Cs 0.7	Ba 0.9	Lu	Hf 1.3	Ta 1.5	W 1.7	Re 1.9	Os 2.2	Ir 2.2	Pt 2.2	Au 2.4	Hg 1.9	Tl 1.8	Pb 1.9	Bi 1.9	Po 2.0	At 2.2			Rn
Fr 0.7	Ra 0.9	Lr	Rf	Db	Sg	Bh	Hs	Mt	Ds	Uuu	Uub	Uut	Uuq	Uup	Uuh	Uus			Uuo

$\longrightarrow$  increasing EN

$\uparrow$  increasing EN

# Electronegativity (EN) 电负性

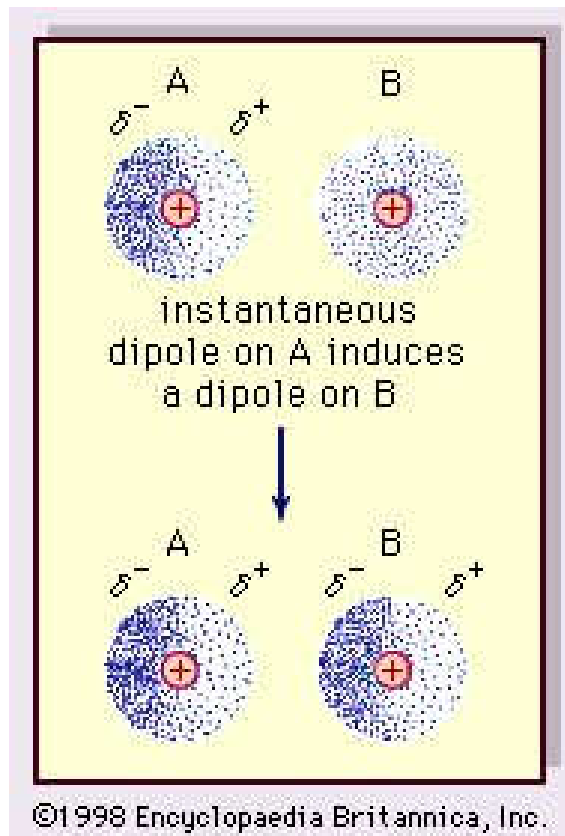
- NaCl has pure ionic bonding
- Silicon has pure covalent bonding
- Solids like GaAs and ZnSe have mixed ionic and covalent bonding



# Van der Waals Bonding 范德华键

- Attraction energy between neutral molecules / atoms

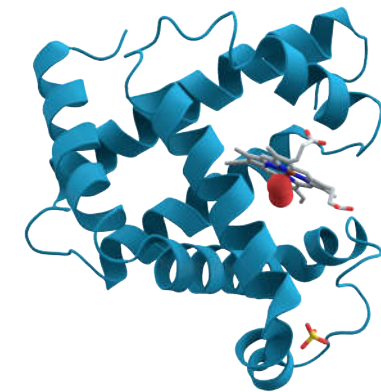
$$U(r) \propto -\frac{1}{r^6}$$



gecko 壁虎



tape



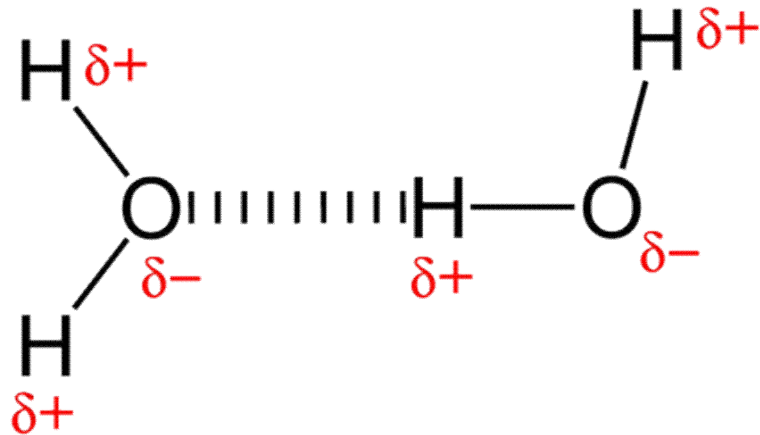
protein

# Hydrogen Bonding 氢键

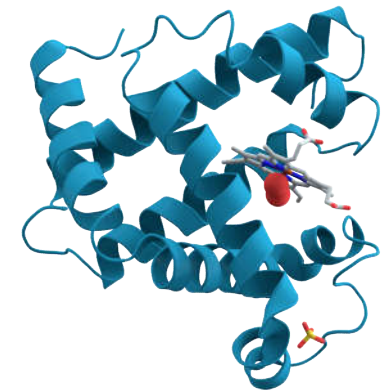
- A special Van der Waals bond
  - generated by hydrogen



water



DNA



protein

# Further Reading

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- **Quantum Mechanics**

- **Physical Chemistry by Mortimer, Chap. 14-16**

- **Atoms and Chemical Bonding**

- **Chemistry: The Central Science, Chap. 6, 8**

- <https://ocw.mit.edu/courses/earth-atmospheric-and-planetary-sciences/12-108-structure-of-earth-materials-fall-2004/lecture-notes/lec5.pdf>

***Thank you for your attention***